

23 **Abstract**

24 Fish growth prediction provides important information for optimising production in aquaculture. Fish
25 usually exhibit different growth characteristics due to the variations in the environment, the equipment
26 used in different fish workshops and inconsistent application by operators of empirical rules varying
27 from one pond to another. To address this challenge, the aim of this study is to develop an adaptive fish
28 growth prediction method in response to feeding decision. Firstly, the practical operational experience in
29 historical feeding decisions for different fish weights is extracted to establish the feeding decision model.
30 Then, a fish weight prediction model is established by regression analysis methods based on historical
31 fish production data analysis. The feeding decision model is integrated as the input information of the
32 fish weight prediction model to obtain fish weight prediction. Furthermore, an adaptive fish growth
33 prediction strategy is proposed by continuously updating model parameters using new measurements to
34 adapt to specific characteristics. The proposed adaptive fish growth prediction method with empirical
35 knowledge extraction is evaluated by the collected production data of spotted knifejaw (*Oplegnathus*
36 *punctatus*). The results show that established models can achieve a good balance between goodness-of-
37 fit and model complexity, and the adaptive prediction method can adapt to specific fish pond's
38 characteristics and provide a more effective way to increase fish weight prediction accuracy. The
39 proposed method provides an important contribution to achieving adaptive fish growth prediction in a
40 real time from the view of aquaculture practice for spotted knifejaw.

41

42 **Keywords:** fish growth prediction; feeding decision making; adaptive update; model adaptation;
43 empirical knowledge extraction; spotted knifejaw

44

Abbreviation	
DEB	Dynamic energy budget
EP	Energy and protein fluxes
DO	Dissolved oxygen
RMSE	Root mean square error
Nomenclature	
<i>BW</i>	Individual fish weight
<i>FR</i>	Feeding ratio
<i>N</i>	Fish number
<i>FA</i>	Total feeding amount
<i>f</i>	Function relationship
<i>p</i> (e.g. <i>a,b,c,d,e</i>)	Function parameter
<i>IFA</i>	Average feeding amount for individual fish

45

46 **1. Introduction**

47 Fish weight is regarded as an important indicator for commercial decision, such as time to market and
48 profit forecast. Fish growth prediction model could provide real-time fish weight information to optimise
49 feeding decision and reduce production cost. For fish growth modelling and fish weight prediction, many
50 research results have been reported. Main modelling approaches include nutrient based models (Belal,
51 2005; Dumas, France, Bureau, 2010; L. Li & Yakupitiyage, 2003), dynamic energy budget (DEB)
52 models (Dambrine et al., 2020; Stavrakidis-Zachou, Papandroulakis, Lika, 2019), and energy and protein
53 fluxes (EP) models (Nobre, Valente, Conceição, Severino, Lupatsch, 2019). However, nutrient based

54 models and DEB models always have complex forms and involve a large number of parameters. It may
55 be difficult to determine the parameters of these mechanistic models accurately in practical production,
56 which limits the practical usage of these models. Although the EP model can extend the traditional
57 bioenergetic model to make the input parameters of model easy to access in fish farms, this model can
58 only be applied to the widely cultured fish species, such as gilthead seabream, European sea bass and
59 white grouper (Lupatsch & Kissil, 2003; Lupatsch & Kissil, 2005; Lupatsch, Kissil, Sklan, 2003) due to
60 the available research results on the relationships analysis for the energy and protein in fish. For many
61 other fish species, their growth characteristics, body composition and growth environment may have
62 great differences. Therefore, for new and small-scale cultured fish species, mechanistic modelling
63 approaches may be not suitable in practice. The data-driven modelling method can be a good alternative
64 approach because there is a wide range of application scenarios in aquaculture, such as water quality
65 monitoring (Yang et al., 2019; Yang, Hassan, Wang, Li, 2017), vaccination effect (Lu, Chen, Yang, Liao,
66 2020), fish counting (Zhang, Li, Liu, Zhou, Duan, 2020), fish mass estimation (Zhang, Wang, Duan,
67 2020), etc. Therefore, this paper pays more attention to the exploration of fish growth prediction method
68 based on the analysis of historical production data from the view of aquaculture practice.

69 In different fish ponds and workshops, there may be deviations in production environment,
70 equipment and feeding decisions from different operators. Therefore, these factors may cause fish in
71 different ponds and workshops to exhibit different growth characteristics. The deviations mainly reflect
72 on fish composition including protein, lipid, ash, moisture and so on, which is shown by the deviation of
73 fish weight finally. After establishing a general fish growth model based on the analysis of historical
74 production dataset, it is necessary to update this model in an adaptive way to decrease the influence of
75 fish weight deviation. The adaptive models can provide an effective approach to adjust model output by

76 using the updated data from specific production environment. Model adaptation methods have been
77 extensively investigated in different fields, such as pharmaceutical manufacturing (Bano, Facco,
78 Ierapetritou, Bezzo, Barolo, 2019), video object segmentation (Sun, Xiao, Lim, Xie, Feng, 2020),
79 unmanned aerial vehicle (Kapteyn, Knezevic, Huynh, Tran, Willcox, 2020), tumour analysis (Tariq,
80 Chen, Kirkby, Jena, 2016) and so on.

81 To predict fish weight, feeding decisions need to be known since they provide very important input
82 information to the prediction of fish weight. Fish feeding is an important operation in aquaculture
83 production. However, making effective fish feeding decisions is a complex task because many factors
84 can affect the decisions that will significantly impact on fish growth. To ensure effective feeding
85 decisions, many studies have explored different methods but they are mainly based on the appetite of
86 fish and their behaviour. Papandroulakis, Markakis, Divanach, and Kentouri (2000) designed a fuzzy
87 logic controller to determine the daily feeding amount of sea bream larvae. There were 316 rules in the
88 fuzzy logic controller, where five linguistic variables were defined to describe population state. Wu,
89 Huang, and Chen (2015) developed an adaptive neural-based fuzzy inference system to make feeding
90 decision by dissolved oxygen (DO) to reflect the appetite of fish. Zhao, Ding, Zhao, and Gu (2019)
91 proposed an adaptive neural fuzzy inference system to make feeding decision based on water quality
92 parameters including DO and temperature. Zhou et al. (2018) proposed a neuro-fuzzy model-based fish
93 feeding decision system by near infrared computer vision and image processing technology. An index to
94 describe fish appetite and quantify feeding behaviour was extracted using image analysis. The review
95 of An, Hao, Wei, Wang, and Yu (2020) summarised the intelligent feeding systems based computer
96 vision technology. Computer vision methods were applied to obtain the changes of fish behaviour (e.g.
97 fishtail swing frequency and movement speed) and the remaining amount of feed. In fish production

98 practice, the common method is to determine feeding amount by fish weight measurement based on
99 operational experience. Because fish biomass is directly related to feeding amount, it has been used to
100 determine daily fish feed demand successfully (Papandroulakis et al., 2000). In practice, fish farming
101 operators divide fish weight into different ranges, and different feeding ratios are determined based on
102 practical experience when fish weight is in different ranges. For fish weight measurement, weighing fish
103 manually every day is both very time consuming and impractical and it often causes damage to fish. As
104 a result, the common practice is to manually measure fish weight only once a month. The feeding decision
105 is adjusted monthly based on new fish weight measurement and its corresponding fish weight range.
106 Although this is a simple and easy way to implement, the adjustment of feeding decision is rough due to
107 the way of fish weight range segmenting and the long gap between two feeding decisions. The adjustment
108 period of feeding decision is restricted by the measurement period of fish weight. This method cannot
109 make feeding decisions based on variable fish weight in real time because of the monthly gaps between
110 two measurement periods. To improve this process, one method is to monitor fish weight and length in
111 real time through installing a video camera based on image analysis technology (Konovalov, Saleh,
112 Efremova, Domingos, Jerry, 2019; Muñoz-Benavent et al., 2018; Shi, Wang, He, Zhang, Li, 2020), but
113 this method will increase equipment and maintenance costs. In addition, the limitations of production
114 environment (e.g. insufficient and uneven illumination condition, high humidity and temperature) can
115 affect the accuracy of image analysis results. Another method is to establish a feeding decision model by
116 analysing historical production data to extract feeding decision operational experience. The latter
117 approach is not fully explored yet, and this paper pays more attention to establishing a feeding decision
118 model based on empirical knowledge extraction by historical production data.

119 In summary, our literature review shows that few studies pay attention to the adaptive fish weight

120 prediction from a view of practical application for the small-scale cultured fish species, spotted knifejaw.
121 It also reveals that a very limited research focuses on the feeding decision modelling based on empirical
122 knowledge extraction to improve feeding decisions and resource efficiency. Therefore, this study aims
123 to address these gaps by proposing an adaptive fish weight prediction method with a feeding decision
124 model based on empirical knowledge extraction in aquaculture.

125 To achieve the research aims, firstly, a feeding decision model was developed by extracting practical
126 operational experience from historical feeding decisions for different fish weights. Three data fitting
127 options were shown to fit this model. A fish weight prediction model was then established by regression
128 analysis methods for historical fish growth production dataset. Three types of modelling methods were
129 considered as options. In modelling process, expert knowledge was introduced to determine input and
130 output variables of model and simplify its form. Subsequently, the real-time fish growth prediction was
131 achieved by integrating feeding decision as the input information of the fish weight prediction model.
132 Finally, an adaptive fish growth prediction strategy was proposed by continuously updating model
133 parameters to adapt to the characteristics change of specific fish pond. The established models and
134 proposed method were parameterised and demonstrated on the collected production dataset of spotted
135 knifejaw (*Oplegnathus punctatus*) from an aquatic company in China to show feasibility. The results
136 show that the established models achieve a good balance between goodness-of-fit and complexity, and
137 the proposed adaptive prediction method can provide an effective way to increase fish weight prediction
138 accuracy and adapt to specific fish pond's characteristics.

139 The novelty of this study is demonstrated from the following aspects: (1) The feeding decision
140 model was established by extracting past practical experience on the premise of not increasing production
141 cost to provide real-time feeding decision. This approach represents a novel attempt in model

142 development as it strengthens the practical applicability and performance of the feeding decision model.
143 (2) The fish weight prediction model was established by regression analysis methods to obtain real-time
144 prediction. This method can ensure to improve its prediction performance by taking consideration of the
145 real time data input obtained in a dynamic fish production environment. (3) To adapt to the specific
146 characteristics of fish pond, the adaptive updating strategy was proposed to enhance its applicability and
147 adaptability in practice. The real-time fish weight prediction can be obtained by responding to feeding
148 decision as input information based on empirical knowledge extraction.

149 In section 2, the practical production dataset of spotted knifejaw is introduced. The feeding decision
150 model and the fish weight prediction model are established by data analysis methods, respectively.
151 Furthermore, the adaptive fish weight prediction method is developed. Section 3 presents model
152 calibration and selection results and the validation of adaptive fish weight prediction method. Section 4
153 provides the conclusions of this study.

154

155 **2. Data acquisition and model development**

156 In this section, the proposed adaptive fish growth prediction method with empirical knowledge extraction
157 is presented in detail, which mainly includes the following three components: (1) a fish feeding decision
158 model, which is used to make feeding decision; (2) a fish weight prediction model, which is applied to
159 predict fish weight at next step in response to feeding decision; (3) an adaptive model updating strategy
160 of fish weight prediction model to adapt to the specific characteristics of fish pond. The framework of
161 adaptive fish growth prediction method with empirical knowledge extraction is shown in Fig. 1.

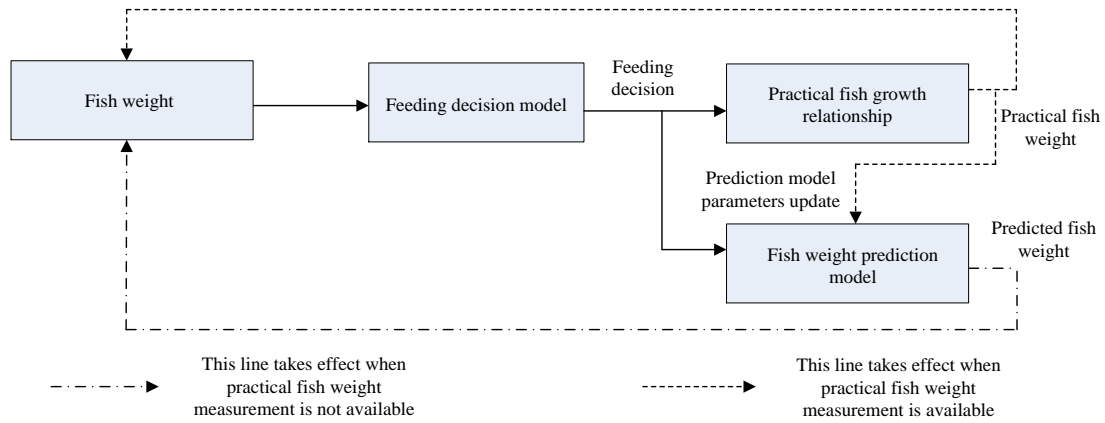


Fig. 1. Framework of adaptive fish growth prediction method with empirical knowledge extraction

The proposed adaptive fish growth prediction method is presented as follows. First, feeding decision is made by the fish feeding decision model based on initial measured fish weight. Then, the fish weight prediction model is used to predict fish weight at next step in response to feeding decision. Finally, fish weight is updated by the obtained fish weight prediction which is used as the new input of fish feeding decision model. Above process is repeated and forms a loop to achieve feeding decision making and fish weight prediction in real time. In this process, when the new fish weight measurement of specific fish pond is available, it is used to update the fish weight prediction model by adjusting model parameters to achieve model adaptation. At the same time, practical measurement is used to update fish weight at next step. Above process is expressed by different lines in Fig. 1. The role of lines in Fig. 1 is distinguished by using different forms based on the availability of fish weight measurements. In the following subsections, fish production datasets, the modelling process of feeding decision model and fish weight prediction model, and the adaptive model updating strategy will be analysed in detail.

2.1 Fish production dataset

In recent years, spotted knifejaw (*Oplegnathus punctatus*) has been introduced and cultured in China,

180 becoming one of the important maricultured fish species because its high nutrition and economic values
181 and taste. However, spotted knifejaw is a newly emerging aquaculture fish species and has not been
182 widely cultured (Kawato, Yamashita, Yuasa, Miwa, Nakajima, 2017). Only a limited number of aquatic
183 companies have carried out artificial breeding and rearing of the species. Studies on spotted knifejaw are
184 still under development. Latest research includes results on immune system analysis (Liu et al., 2019;
185 Zhang et al., 2020), genetic sex identification (Li et al., 2020), fish length estimation (Shi et al., 2020),
186 environment effects (Yang, Song, Peng, Hallerman, Huang, 2019). This study focuses on the growth
187 characteristics of spotted knifejaw. The production dataset of spotted knifejaw from an aquatic company
188 is applied to fit and verify proposed method. The aquatic company was a land-based factory using a
189 closed recirculating marine aquaculture system located in the Laizhou Bay of China. In this factory, every
190 workshop was occupied about 20 fish ponds. The workers in this factory collected the production data
191 from seven workshops for one year and carried out a statistical analysis for mass production data. The
192 obtained datasets were characterised by the statistical average method when fish were at the same growth
193 stage. Finally, 33 the production datasets of spotted knifejaw from seven workshops provided by factory
194 were supplied for modelling and verification as shown in Table 1. The collected variables in the
195 production datasets of spotted knifejaw include individual fish weight, fish number, total feeding amount
196 and cultured time.

197

198

199 Table 1 The production datasets of spotted knifejaw

Data number	Initial individual fish weight (g)	Individual fish weight at the end of cultured time	Fish number	Total feeding amount (g)	Cultured time (day)
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(g)					
1	145	205	1450	4500	31
2	205	270	1450	4500	30
3	270	330	1450	5500	31
4	330	405	1309	5500	30
5	40	53	2778	2800	30
6	53	75	2778	3200	31
7	50	90	2479	4500	30
8	90	145	2479	5000	31
9	145	200	2479	6000	31
10	200	265	1500	4500	30
11	265	330	1500	6000	31
12	330	400	1375	5500	30
13	660	725	902	2145	31
14	725	735	873	2195	30
15	170	220	1723	5515	30
16	575	645	1237	5325	31
17	645	680	1237	5155	30
18	225	260	1072	3025	31
19	660	790	1171	6655	31
20	750	785	1098	5485	30
21	785	825	1088	5485	31

22	225	260	1294	3950	31
23	260	330	1287	5350	28
24	310	385	1183	5500	31
25	520	560	934	3875	31
26	175	195	2690	6285	30
27	195	235	2690	6530	31
28	235	285	1343	3585	30
29	585	690	1380	6910	31
30	690	755	1363	5770	30
31	755	780	1363	5770	31
32	35	43.5	5015	2000	30
33	43.5	55	4934	3435	31

200

201 **2.2 Fish feeding decision model**

202 In traditional fish production practice, the adjustment period of feeding decision is the same as the period
 203 of manual fish weight measurement, which is once a month. The specific process of fish feeding decision
 204 is described as follow: once a month some cultured fish are sampled in a random way and weighed to
 205 estimate the average fish weight in the same fish pond. The operators determine the feeding ratio for the
 206 range of measured fish weight based on past operational experience. The feeding amount is based on fish
 207 weight, feeding ratio and fish number, which is calculated by Eq. (1).

$$208 \quad FA = BW \times FR \times N \quad (1)$$

209 where BW (g) is individual fish weight in a fish pond. FR (%) represents the feeding ratio and FA

210 (g) is total feeding amount in a fish pond. N represents cultured fish number in a fish pond. In general,
 211 the initial total cultured fish number in a fish pond is known. As production proceeds the change of fish
 212 number can be recorded by subtracting death number from the initial total number of fish. The
 213 determination principle of feeding ratio FR is that larger fish weight requires a smaller feeding ratio.
 214 The specific value of feeding ratio is set based on the growth characteristics of cultured fish, which is
 215 from operational experience. Although this is a simple and easy way to implement for operators in
 216 practical production, the simple division of fish weight range results in rough feeding decisions. Also,
 217 the measurement period of fish weight restricts the adjustment frequency of feeding decision. The real-
 218 time feeding decisions cannot be made for variable fish weight in a timely manner because of the long
 219 gaps between two fish weight measurements. Therefore, this study considers extracting operational
 220 experience by the analysis of historical fish feeding decisions. The fish feeding decision model was
 221 established to obtain feeding decision in real time from a practical application point of view. The feeding
 222 ratio FR was obtained by Eq. (2).

$$223 \quad FR = f(BW, p) \quad (2)$$

224 where f is the function relationship between BW and FR . p is function parameter. The relationship
 225 f is obtained by the analysis of historical fish feeding decisions, which is fitted by different functions
 226 as options to choose more suitable one. The following three models were adopted to fit the relationship
 227 f and mimic reality, which are shown in Eqs. (3)-(5).

$$228 \quad f_1(x) = a_1 \times e^{-b_1 \times x} + c_1 \quad (3)$$

$$229 \quad f_2(x) = a_2 \times x^{-b_2} \quad (4)$$

$$230 \quad f_3(x) = \frac{a_3}{x + b_3} \quad (5)$$

231 where x represents BW . $f_i(x)$ ($i = 1, 2, 3$) represents FR . a_i ($i = 1, 2, 3$), b_i ($i = 1, 2, 3$) and c_1

232 represent p . Above three functions all meet the determination principle of feeding ratio, that is to say, a
233 larger fish weight needs a smaller feeding ratio.

234

235 **2.3 Fish weight prediction model**

236 The fundamental task in fish growth control research is to understand and predict fish weight in response
237 to feeding decision. For fish weight monitoring, the widely used method is to catch some fish by fishing
238 net once a month and weigh them to calculate average fish weight in a fish pond. It is time consuming
239 and impractical to weigh fish manually every day and manual weighing can cause damage to fish. The
240 low measurement frequency of fish weight makes real-time fish growth monitoring difficult. Therefore,
241 it is necessary to develop the fish weight prediction model to achieve real-time fish weight monitoring.

242 The availability of feeding amount, fish weight, fish number and cultured time in historical production
243 dataset makes the establishment of fish weight prediction model become possible. In this section, based
244 on the analysis of historical production dataset from many ponds and workshops, a fish weight prediction
245 model is established to predict fish weight in response to feeding decision in real time, which can provide
246 timely indication of fish growth. The fish weight prediction model is expressed by Eq. (6)

$$247 \quad BW_t = f_g(BW_0, FA, t, N, p_g) \quad (6)$$

248 where BW_0 represents initial individual fish weight. t (day) is cultured time. p_g is the parameter of
249 function f_g . BW_t is individual fish weight at any given point in time (t).

250 The following three methods are used to determine relationship f_g :

251 **Method 1:** This method is performed using a multiple linear regression approach. The input variables
252 include BW_0 , FA , t and N , and the output variable is BW_t . It is expressed as shown in Eq. (7).

$$253 \quad BW_t = a_{g1} \times BW_0 + b_{g1} \times FA + c_{g1} \times t + d_{g1} \times N + e_{g1} \quad (7)$$

254 In this method there are many parameters in the model described in Eq. (7). To simplify the form of
 255 model and decrease the number of parameters, expert knowledge and operational experience are
 256 introduced to determine input and output variables, which are shown in the following two methods.

257 **Method 2:** The second method uses the same multiple linear regression approach as the first method, but
 258 it has different input and output variables. The input variables include BW_0 and average feeding amount
 259 for individual fish IFA which is shown as Eq. (8), and the output variable is the increment of fish
 260 weight per day BW_z , which is calculated by Eq. (9).

$$261 \quad IFA = \frac{FA}{N} \quad (8)$$

$$262 \quad BW_z = \frac{BW_t - BW_0}{t} \quad (9)$$

263 Therefore, the relationship between input variables (BW_0 and IFA) and output variable BW_z is fitted
 264 by Eq. (10). The relationship f_g can be determined indirectly by Eqs. (8)-(10).

$$265 \quad BW_z = a_{g2} \times BW_0 + b_{g2} \times IFA \quad (10)$$

266 **Method 3:** This method uses linear regression approach which is shown as Eq. (11). Because BW_z
 267 includes the information of BW_0 , the number of input variables for Eq. (10) is reduced to one, and the
 268 output variable is the same as Method 2.

$$269 \quad BW_z = a_{g3} \times IFA + b_{g3} \quad (11)$$

270 Table 2 summarises the modelling options for fish weight prediction model.

271

272

Table 2. Modelling options for fish weight prediction model

Modelling methods	Eqs.	Parameters
Method one (multiple linear regression)	(7)	$a_{g1}, b_{g1}, c_{g1}, d_{g1}, e_{g1}$
Method two (multiple linear regression)	(8), (9), (10)	a_{g2}, b_{g2}

Method three (linear regression)

(8), (9), (11)

a_{g3}, b_{g3}

273

274 Above fish feeding decision model and fish weight prediction model were integrated to make
275 feeding decision and predict fish weight in real time. The models were parameterised using the historical
276 production dataset of spotted knifejaw. The feeding decision model and fish weight prediction model
277 options in sections 2.2 and 2.3 were calibrated to the production datasets of spotted knifejaw by
278 estimating model parameters. Root mean square error (RMSE) between measurement and model fitting
279 was used to assess model goodness-of-fit. The final model form was selected by balancing goodness-of-
280 fit and model complexity. The fitting parameters and performance comparison of different model options
281 and final chosen model will be shown in section 3.

282 For the representation of dynamic model, the most common approach is autoregressive modelling.
283 Taking the simplest first order linear autoregressive format as the example, in this study, the input variable
284 is average feeding amount for individual fish and the state variable is individual fish weight. The fish
285 weight at a specific time was expressed as Eq. (12).

$$286 \quad BW_t = a \times BW_{t-1} + b \times IFA \quad (12)$$

287 where a and b are the model parameters which need to be estimated. In this study, the objective was
288 to obtain fish weight prediction every day. Using autoregressive model Eq. (12), the historical fish weight
289 measurement every day needed to be available. However, in the historical production dataset of spotted
290 knifejaw, only fish weight measurement once a month was available. Therefore, based on the
291 characteristics of historical production dataset, above “Method 1” to “Method 3” in this study were used
292 to fit fish weight prediction model. For Method 3, the model was transformed into the following form in
293 Eq. (13) based on Eqs. (8), (9) and (11).

294
$$BW_t = (BW_0 + b_{g3} \times t) + a_{g3} \times t \times IFA \quad (13)$$

295 The fish weight at $t-1$ time point is expressed as Eq. (14).

296
$$BW_{t-1} = (BW_0 + b_{g3} \times (t-1)) + (a_{g3} \times t \times IFA - a_{g3} \times IFA) \quad (14)$$

297 Based on Eqs. (13) and (14), fish weight at t time point was described as in Eq. (15).

298
$$BW_t = BW_{t-1} + a_{g3} \times IFA + b_{g3} \quad (15)$$

299 By comparing Eq. (12) with Eq. (15), Method 3 in this study had a similar form to the typical dynamic
300 model.

301

302 **2.4 Adaptive prediction strategy**

303 Because of the variability of specific fish pond characteristics, the developed fish weight prediction
304 model using historical production datasets may not adapt to the production of a new specific fish pond.

305 The concept of adaptive updating provides a way to solve above problem. Model adaptation is used to
306 ensure the prediction performance of fish weight for specific fish pond. This section presents an adaptive

307 model updating method for fish weight prediction model. The main idea of adaptive prediction of fish
308 growth is to improve the prediction of fish weight in response to feeding decision by using the collected

309 measurements of the specific fish pond. When a new specific fish pond is used as research target, the
310 adaptive prediction process is described as below.

311 At the initial stage, the established fish weight prediction model by historical production dataset is
312 applied to predict fish weight. When the specific fish pond production data was available, the parameters
313 of established fish weight prediction model were updated by fitting new measurements of specific fish
314 pond to achieve a smooth transition from a general model to a specific model in an adaptive manner.

315 Bayesian theory could be used to interpret our proposed adaptive model updating method. For the

316 determination of model parameters, our proposed method included two aspects of information. The
317 model parameters were obtained by historical production dataset analysis, which were regarded as prior
318 parameters. On the other hand, the actual fish weight measurement of specific fish pond provided new
319 information to update the parameters of established fish weight prediction model, which was regarded as
320 posterior parameters. During an ongoing fish production process, more actual fish weight measurements
321 of the specific fish pond will be used to update model parameters in an adaptive manner, which makes
322 the model more adaptive to the specific characteristics and increases the accuracy of fish weight
323 prediction.

324 For the relationship between general model and specific model, there are three situations: (1) all the
325 specific model characteristics are included in the general model, or (2) there is a certain amount of
326 overlap for the characteristics of two models, or (3) there is significant difference for the characteristics
327 of two models. Therefore, in the results and discussion section, the following three scenarios are
328 simulated to show the performance of proposed adaptive prediction method for different conditions.

329 **Scenario 1:** all the characteristics of specific fish pond are considered in the general model.

330 **Scenario 2:** part characteristics of specific fish pond are considered in the general model.

331 **Scenario 3:** no information of specific fish pond is covered in the general model.

332 To demonstrate our proposed method, the proposed adaptive prediction method was compared with
333 the following two methods to demonstrate effectiveness including (1) only using the prediction model
334 with no adaption for specific fish pond (This method is denoted as “no adaptation”) and (2) only using
335 limited measurements from specific fish pond to establish model for fish weight prediction (This method
336 is denoted as “no prediction”). All three situations were simulated to show the performance of proposed
337 adaptive prediction method under different conditions. The model prediction method with no adaptation

338 provided the baseline results against the performance of proposed adaptive prediction model.

339

340 **2.5 The implementation of adaptive fish growth prediction method**

341 The implementation process of adaptive fish growth prediction method is shown in Fig. 2. To achieve

342 the real-time fish weight prediction in aquaculture, the implementation steps were presented as follows.

343 **Step 1:** Fish weight is used as input of feeding decision model to obtain feeding decision.

344 **Step 2:** Feeding decision is used to predict fish weight based on the fish weight prediction model.

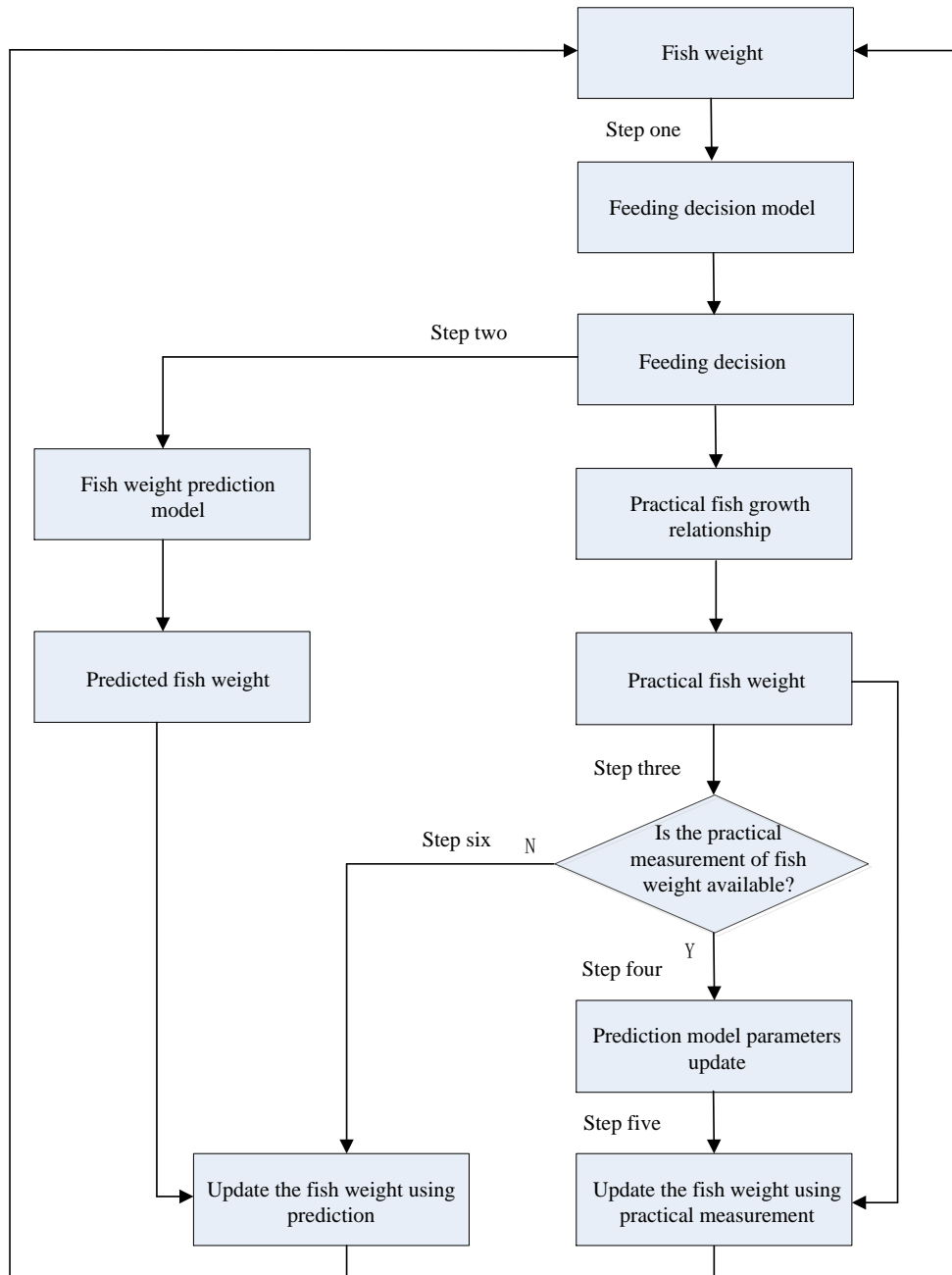
345 **Step 3:** Judge whether the practical measurement of fish weight is available or not. If the answer is “Yes”,

346 shift to Step 4. If the answer is “No”, shift to Step 6.

347 **Step 4:** The parameters of fish weight prediction model is updated.

348 **Step 5:** Update fish weight using the practical measurement. Shift to Step 1.

349 **Step 6:** Update fish weight using the prediction result. Shift to Step 1.



350

351

Fig. 2. Implementation process of adaptive fish growth prediction method

352

353 3. Results and discussion

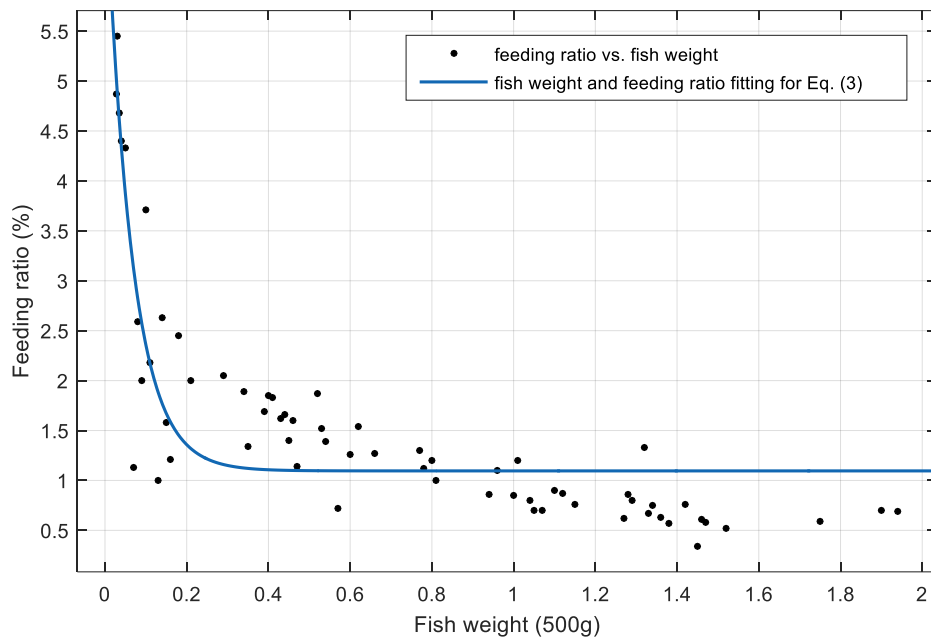
354 Two sets of results are shown in this section. One set of results is for model calibration and selection, and

355 another set of results is for the adaptive fish weight prediction.

356

357 **3.1 Model calibration and selection results**

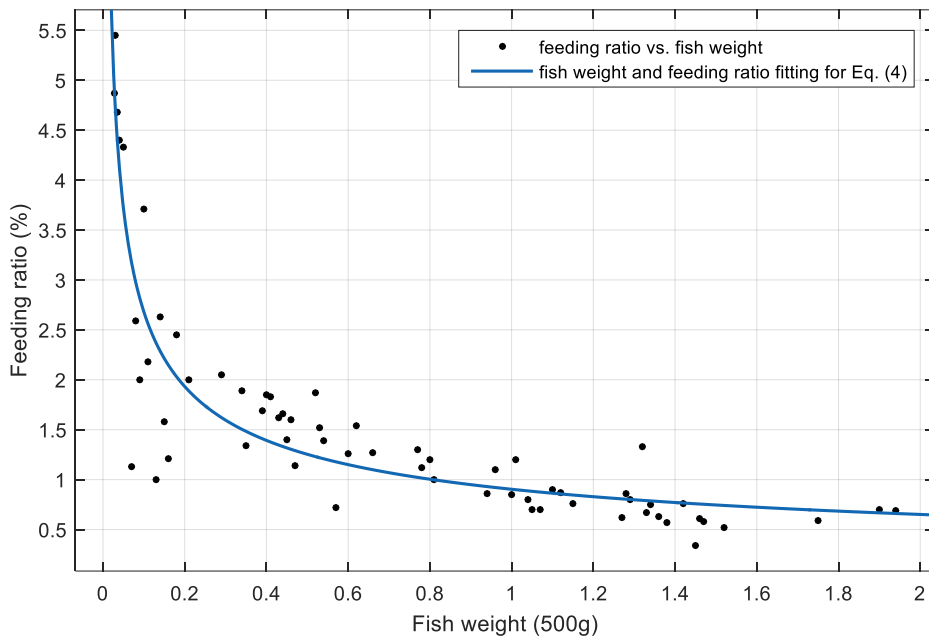
358 Model fitting plots for the fish feeding decision model options are shown in Fig. 3. The horizontal axis
359 represents individual fish weight. The vertical axis represents feeding ratio which is a percentage (%).
360 The calibration results of three options (Eqs. (3), (4) and (5)) for fish feeding decision model are shown
361 in Table 3, including estimated parameters and RMSE. According to RMSE, the second model (Eq. (4))
362 has the minimum RMSE and a better goodness-of-fit performance. However, it does not include more
363 parameters compared with other two models (Eqs. (3) and (5)). Therefore, the model 2 (Eq. (4)) appears
364 to be a good representation for fish feeding decision making.



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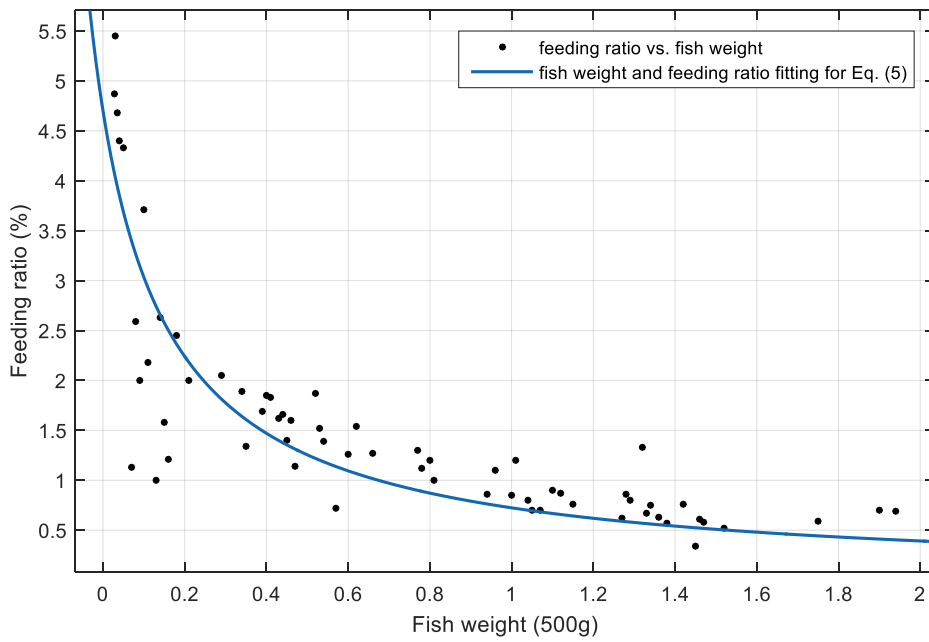
(a)



367

368

(b)



369

370

(c)

371 Fig. 3. Fitted feeding ratio against practical value for the feeding decision model options (a) model 1

372 (Eq. (3)), (b) model 2 (Eq. (4)) and (c) model 3 (Eq. (5))

373

374

Table 3. The calibration results for fish feeding decision model

Models	Parameters	RMSE
	$a_1=6.084$ [4.481, 7.686]	
Eq. (3)	$b_1 = 15.72$ [10.4, 21.03]	0.5577
	$c_1 = 1.096$ [0.9339, 1.257]	
	$a_2=0.9037$ [0.7796, 1.028]	
Eq. (4)	$b_2 = 0.4722$ [0.4193, 0.5252]	0.4721
	$a_3=0.8559$ [0.6523, 1.06]	
Eq. (5)	$b_3 = 0.1821$ [0.1162, 0.248]	0.5854

375

376 The calibration results of three options for fish weight prediction model are shown in Table 4,
377 including the estimated parameters and RMSE. The first model (Method 1) with more parameters
378 achieves better goodness-of-fit than other two models with simple form (Methods 2 and 3). The second
379 model (Method 2) and the third model (Method 3) had similar fitting accuracy, which are from the
380 simplification by expert knowledge and operational experience. For input variables, the introduction of
381 initial individual fish weight provided very little benefit (RMSE was reduced from 0.1698 (Method 3) to
382 0.1694 (Method 2)), and improvement was not substantial. Therefore, the analysis for the input variables
383 of the third model (Method 3) was reasonable. The initial individual fish weight can be removed from
384 input variables, and the model form simplified. By trading off goodness-of-fit and model complexity, the
385 third model (Method 3) appeared to be a more reasonable choice because of its straightforward
386 implementation.

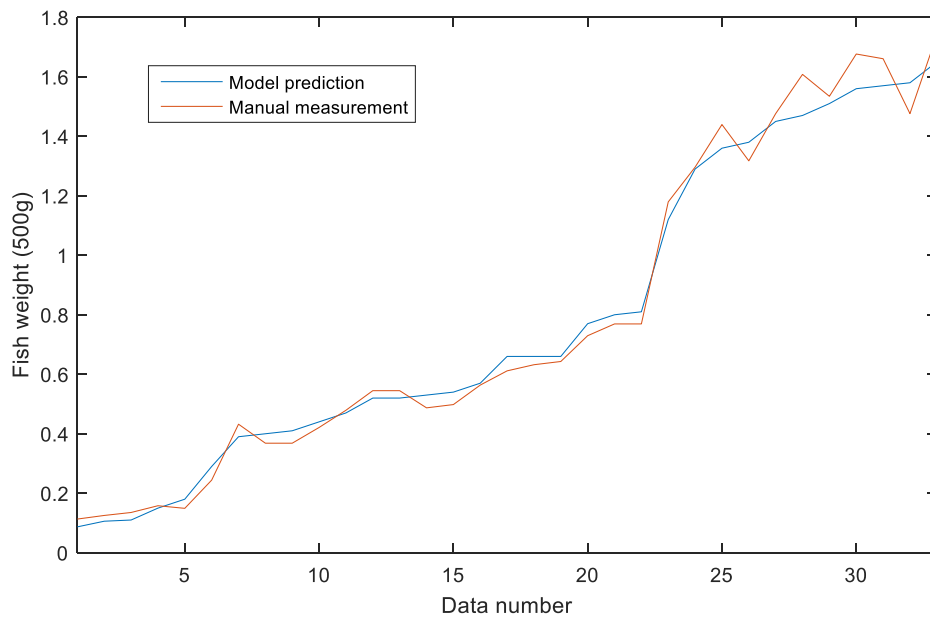
387

Table 4. The calibration results for fish weight prediction model

Modelling methods	Parameters	RMSE
Method 1	$a_{g1}=0.5724, b_{g1}=0.1242, c_{g1}=0.0867,$ $d_{g1}=-0.2021, e_{g1}=0.1202$	0.1048
Method 2	$a_{g2}=0.031646, b_{g2}=0.587013$	0.1694
Method 3	$a_{g3}=0.5908, b_{g3}=0.03239$	0.1698

389

390 Fish weight was predicted by integrating the fish feeding decision model and the fish weight
 391 prediction model, and the prediction results were compared with fish weight measurements, which are
 392 illustrated in Fig. 4. The RMSE between prediction and measurement is 0.0543. Note that the established
 393 models can make feeding decision and predict fish weight effectively. The selected modelling option
 394 provided satisfactory results.



395

396

Fig. 4. Comparison between model prediction and manual measurements

397 **3.2 Adaptive prediction results**

398 If the specific fish pond has unique characteristics that are not adequately covered in the general model,
399 the general model has limited ability to predict fish weight. The general model thus needs to be updated
400 by the measurement of specific fish pond to adapt to its variations. In this study, 25 datasets from six
401 workshops were used as the historical datasets for modelling, and 8 datasets from one workshop were
402 used as the measurements from a specific fish pond and workshop to verify the proposed fish weight
403 prediction method. Table 5 shows the RMSE of different fish weight prediction methods compared with
404 fish weight measurements including proposed adaptive prediction method, general model prediction (i.e.
405 no adaptation), and model fitting using limited new measurements (i.e. no prediction). The results of
406 adaptive prediction are presented by using the selected fish feeding decision model (Eq. (4)) and fish
407 weight prediction model (Method 3). It can be seen that proposed adaptive prediction method can update
408 the parameters of general model and provide better fish weight prediction performance compared with
409 other two methods. The general model had certain deviations compared with the specific fish pond. If no
410 adaptive measures are implemented, then the prediction performance of general model will decline.
411 When the new measurements of specific fish pond are very limited, it is difficult to represent the
412 characteristics of specific fish pond accurately. Therefore, the prediction performance of “no prediction”
413 is worse than other two methods.

414

415

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417

418

419 Table 5 The RMSE of different fish weight prediction methods compared with fish weight

420

measurements	
Modelling methods	RMSE
Proposed adaptive prediction method	0.0617
No adaptation	0.0622
No prediction	0.3459

421

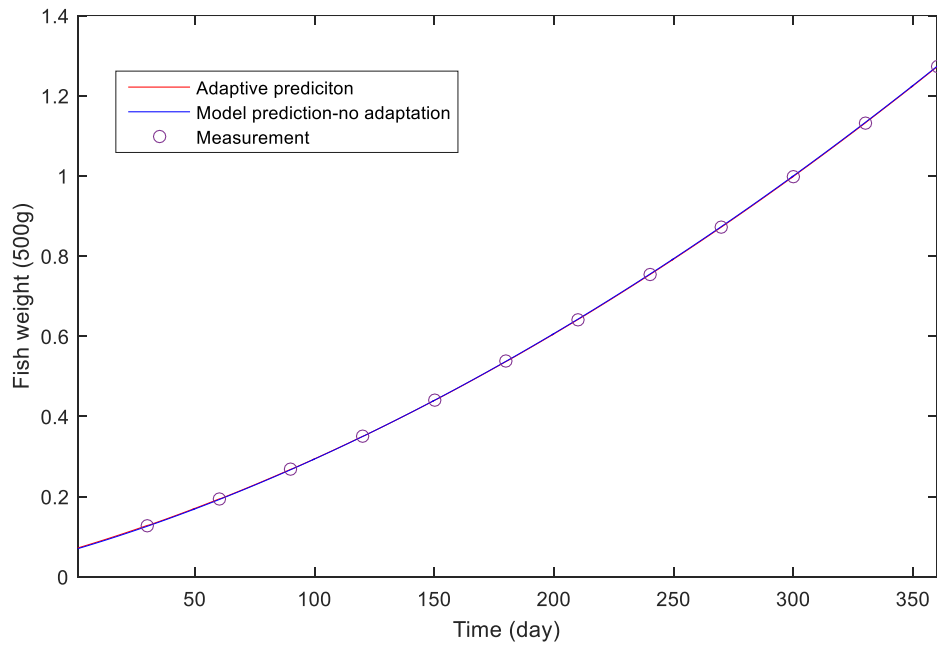
422 For the relationship between general model and specific model, the three situations in section 2.4

423 were simulated to show the performance of proposed adaptive prediction method in different conditions.

424 The comparison results of proposed adaptive prediction method and model prediction with no adaptation

425 for different situations are illustrated in Fig. 5. Because the growth period of spotted knifejaw occurs

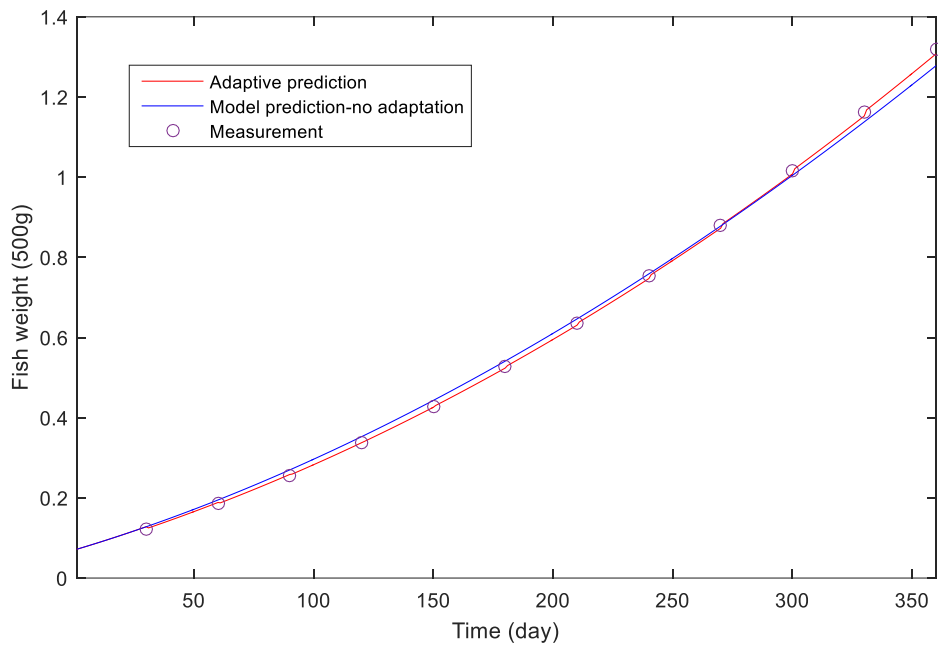
426 over about one year, the simulated cultured time was set as 360 d.



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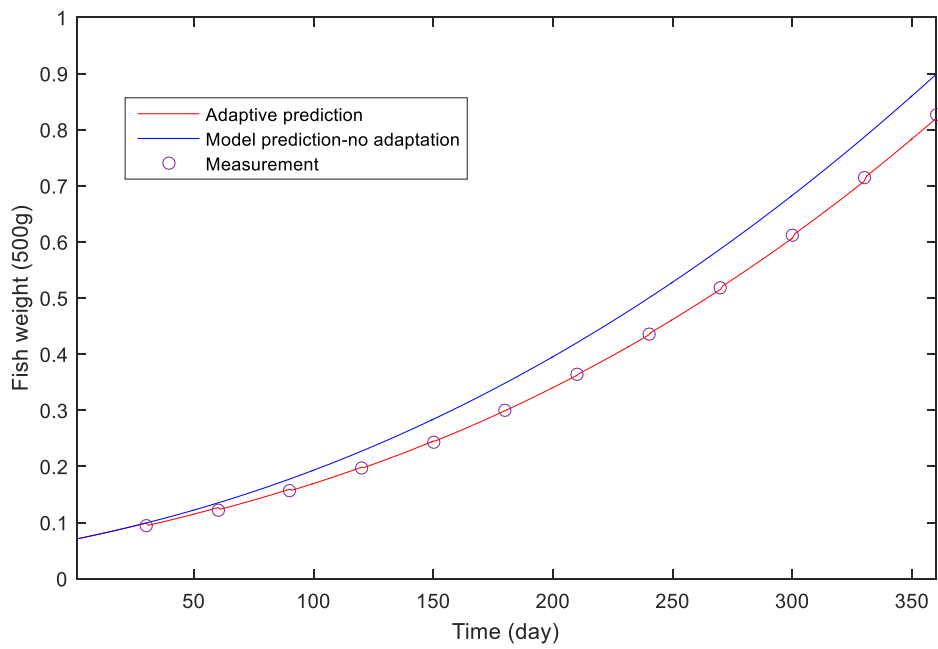
(a)



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(b)



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(c)

433 Fig. 5. Comparison results of fish weight prediction for different situations (a) scenario 1, (b) scenario

434

2 and (c) scenario 3

435

436 The fish weight measurement period is set as once a month, so for proposed adaptive predication
437 method, the parameter updating period is once a month. In practical production process, the measured
438 fish weight curve is unknown, and only the measurements once a month are available. To compare
439 performances, Fig. 5 shows the simulation results of different situations. The RMSEs of adaptive
440 prediction model and model prediction with no adaptation for different situations are shown in Table 6.
441 It is noted that the adaptive prediction method improves the prediction performance to various extents
442 for different situations. When all the characteristics of specific fish pond are covered in the general model
443 (scenario 1), the model prediction with no adaptation performs well for a specific fish pond. The RMSEs
444 of two methods are all very small. When the specific fish pond owns great differences compared with
445 the general model (scenario 3), the improvement in prediction accuracy becomes more apparent.
446 Scenario 2 is the middle degree. The performances of model prediction with no adaptation rely on the
447 similarity between general model and specific fish pond. When the general model has a bigger similarity
448 compared with specific fish pond, it will achieve better prediction performance for the specific fish pond
449 with no adaptation. Inversely, when the similarity is low, the improvement role of proposed adaptive
450 prediction method will be greater.

451

452 Table 6 The RMSEs of adaptive prediction model and model prediction with no adaptation for different
453 situations

Condition	RMSE of adaptive prediction model	RMSE of model prediction with no adaptation
scenario 1	0.0004	0.0042
scenario 2	0.0062	0.0166
scenario 3	0.0038	0.0498

454

455 **3.3 Discussion**

456 By trading off goodness-of-fit and model complexity, the feeding decision model and the fish weight
457 prediction model can be determined from available options. It should be noted that a complex model
458 with a large number of free parameters would fit historical dataset better than a simpler one. However,
459 complex models tend to over fit data and generalisation is not good enough. In addition, to adapt to the
460 small amount of specific fish pond data quickly, the complex model form with too many parameters is
461 not suitable. The proposed adaptive fish weight prediction method achieves a better performance
462 compared with the methods including “no adaptation” and “no prediction”, which not only maintains the
463 general characteristics from historical dataset, but also adapts to the specific characteristics from new
464 fish pond. When adaptive prediction method is compared with “no prediction” method, the RMSE
465 decreases 82.16%. The improvement degree of adaptive prediction method depends on the deviations
466 between general characteristics and specific characteristics. More obvious deviations will show greater
467 improvement role. When adaptive prediction method is compared with model prediction with no
468 adaptation, the RMSE for different situations decreases 81.82% averagely.

469 In summary, the proposed adaptive fish growth prediction method with empirical knowledge
470 extraction can reduce the impact of knowledge differences among different operators and provide real-
471 time fish growth prediction for the dynamic production environment in an adaptive way.

472

473 **4. Conclusions**

474 In this study, an adaptive fish growth prediction method with empirical knowledge extraction was
475 developed. The feeding decision model was established by extracting practical operational experience

476 from historical production data. The fish weight prediction method was proposed using regression
477 analysis. The feeding decision was used as the input information of the fish weight prediction method to
478 obtain real-time prediction and adapted to the specific characteristics of new fish ponds. An adaptive
479 updating strategy was proposed by continuously updating model parameters with new measurements.
480 The proposed method was evaluated by the collected production dataset of spotted knifejaw. The results
481 show that the fish growth prediction method can obtain real-time fish weight prediction in response to
482 feeding decision based on empirical knowledge extraction. The adaptive prediction method provides an
483 effective way to increase fish weight prediction accuracy and adapt to the specific fish pond's
484 characteristics.

485 This study can significantly contribute to the real-time fish growth prediction in aquaculture practice.
486 However, this research has a few limitations that provide opportunities for future research. For example,
487 in the process of feeding decision modelling, only fish weight is considered as the main factor for feeding
488 decision. Future work may focus on exploring more other factors related with feeding decision to
489 improve feeding decision, e.g. water quality parameters. In addition, the proposed adaptive strategy is a
490 simple updating way by adjusting model parameters using new measurements. It is an important direction
491 to increase the accuracy of adaptive fish weight prediction by improving model updating strategy further.

492

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607 **Figure captions**

608 Fig. 1. Framework of adaptive fish growth prediction method with empirical knowledge extraction

609 Fig. 2. Implementation process of adaptive fish growth prediction method

610 Fig. 3. Fitted feeding ratio against practical value for the feeding decision model options (a) model 1 (Eq.

611 (3)), (b) model 2 (Eq. (4)) and (c) model 3 (Eq. (5))

612 Fig. 4. Comparison between model prediction and manual measurements

613 Fig. 5. Comparison results of fish weight prediction for different situations (a) scenario 1, (b) scenario 2

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